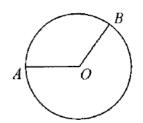
# www.mymathscloud.com

## CORE MATHEMATICS (C) UNIT 2 TEST PAPER 6

- 1. Use the trapezium rule with three intervals to estimate  $\int_{2}^{5} \sqrt{2x^{2}-1} dx$  to 1 decimal place. [4]
- 2. Geri's uncle gave her £3 on her first birthday. Subsequently he gave her £(2n + 1) on her nth birthday, until her 18<sup>th</sup> birthday. How much did he give her altogether? [4]
- The diagram shows a circle with center O and radius 8 cm.
  The minor sector AOB has perimeter 36 cm. Calculate
  (i) the angle AOB, in radians,
  - (ii) the area of the sector AOB, in cm<sup>2</sup>. [2]

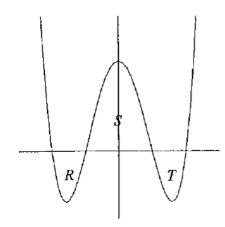


- 4. The third term of a geometric series is 160 and the eighth term is 5. Find
  - (i) the common ratio, [2]
  - (ii) the first term, [2]
  - (iii) the sum to infinity of the series. [2]
- 5.  $f(x) \equiv \log_2 (4-x^2), -2 < x < 2.$ 
  - (i) Find f(1) to 2 decimal places. [2]
  - (ii) Express  $f(x) \log_2(2 x)$  in its simplest form. [3]
  - (iii) Solve for x the equation f(x) = -1. [2]
- 6. (i) Expand  $(1-2x)^9$  in ascending powers of x as far as the term in  $x^3$ . [4]
  - (ii) By substituting a suitable value for x in your expansion, obtain an estimate of  $0.98^9$ . [3]
- 7. The gradient at the point (x, y) on a curve C is equal to  $x^{\frac{3}{2}}$ . The curve passes through the point P(4, 13). Find
  - (i) the equation of C, in the form y = f(x), [4]
  - (ii) an equation of the normal to C at P, in the form ax + by + c = 0. [5]
- 8. (i) Divide  $(4x^3 2x^2 8x + 5)$  by (2x 3). [5]
  - (ii) Given that the remainder when  $(x^2 6x 27)$  is divided by (x k) is positive, find the set of possible values of k. [4]

### CORE MATHEMATICS 2 (C) TEST PAPER 6 Page 2

- 9. The equation of a curve is  $y = 2 \sin \left(x + \frac{2\pi}{3}\right)$ .
  - (i) Find the values of x in the interval  $0 \le x \le 2\pi$  at which the curve cuts the x-axis. [4]
  - (ii) Sketch the curve for  $0 \le x \le 2\pi$ , clearly showing the values found in part (i) and giving the coordinates of any maximum and minimum points in terms of  $\pi$ . [5]
- 10.  $f(x) \equiv x^4 5x^2 + 4$ .
  - (i) By using the substitution  $t = x^2$ , or otherwise, factorise f(x) completely. [4]

The diagram shows the graph of y = f(x).



- (ii) Write down the coordinates of all the points wherethe curve meets the x-axis. [2]
- (iii) Calculate the total area of the regions R, S and T between the curve and the x-axis. [7]

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## CORE MATHS 2 (C) TEST PAPER 6: ANSWERS AND MARK SCHEME

1. 
$$(2, 2.646), (3, 4.123), (4, 5.568), (5, 7)$$
  $\frac{1}{2}(9.646 + 2(9.691)) = 14.5$  B2 M1 A1

2. Sequence is 3, 5, 7, ..., 37 Sum = 
$$9(40) = £360$$
 M1 A1 M1 A1 4

3. (i) 
$$16 + 8\theta = 36$$
  $\theta = 2.5$  radians (ii) Area =  $\frac{1}{2}$  (64)(2.5) = 80 cm<sup>2</sup> M1 A1 M1 A1 4

4. (i) 
$$r^5 = 1/32$$
  $r = 1/2$  (ii)  $a(1/2^2) = 160$   $a = 640$  M1 A1 M1 A1 (iii)  $a/(1-r) = 1280$  M1 A1 6

5. (i) 
$$f(1) = \log_2 3 = \log 3 / \log 2 = 1.59$$
 M1 A1  
(ii)  $\log_2 ((4 - x^2)/(2 - x)) = \log_2 (2 + x)$  M1 A1 A1  
(iii)  $4 - x^2 = \frac{1}{2}$   $x = \sqrt{7/2}$  (= ±1.87 to 2 decimal places) M1 A1

6. (i) 
$$(1-2x)^9 = 1 + 9(-2x) + 36(-2x)^2 + 84(-2x)^3 + \dots$$
 M1 M1  
 $= 1 - 18x + 144x^2 - 672x^3 + \dots$  A1 A1  
(ii) Put  $x = 0.01$  to get  $1 - 0.18 + 0.0144 - 0.000672 = 0.833728$  M1 A1 A1

7. (i) 
$$y = \frac{2}{5}x^{5/2} + c$$
  $13 = \frac{64}{5} + c$   $y = \frac{2}{5}x^{5/2} + \frac{1}{5}$  M1 A1 M1 A1  
(ii) Gradient at  $P = 8$ , so normal is  $y - 13 = -1/8(x - 4)$  B1 M1 A1  
 $8y - 104 = 4 - x$   $x + 8y - 108 = 0$  M1 A1 9

8. (i) Long division gives 
$$2x^2 + 2x - 1 + \frac{2}{2x - 3}$$
 M1 A1 A1 A1 A1 A1 (ii)  $k^2 - 6k - 27 > 0$   $(k+3)(k-9) > 0$   $k < -3$  or  $k > 9$  M1 A1 M1 A1 9

9. (i) When 
$$y = 0$$
,  $x + 2\pi/3 = \pi$ ,  $2\pi$   $x = \pi/3$ ,  $x = 4\pi/3$  M1 A1 M1 A1 (ii) Graph thro'  $(\pi/3, 0)$ ,  $(4\pi/3, 0)$ ; min. at  $(5\pi/6, -2)$ , max. at  $(11\pi/6, 2)$  B1 B2 B2 9

10. (i) 
$$f(x) = (t-1)(t-4) = (x^2-1)(x^2-4) = (x+1)(x-1)(x+2)(x-2)$$
 M1 A1 M1 A1  
(ii)  $(-2, 0), (-1, 0), (1, 0), (2, 0)$  B1 B1

(iii) 
$$R = T = \int_{1}^{2} (x^{4} - 5x^{2} + 4) dx = \left[ \frac{x^{5}}{5} - \frac{5x^{3}}{3} + 4x \right]_{1}^{2} = \frac{31}{5} - \frac{35}{3} + 4 = -\frac{22}{15}$$
 M1 A1 A1
$$S = 2 \int_{0}^{1} (x^{4} - 5x^{2} + 4) dx = 2 \left[ \frac{x^{5}}{5} - \frac{5x^{3}}{3} + 4x \right]_{1}^{1} = \frac{76}{15}$$
 Total area = 8 M1 A1 A1 A1